

## Clustering Algorithms

WS 2015/2016

Handout 6

**Exercise 1:**

Given a set of  $P \subset M$  and  $k \in \mathbb{N}$  ( $|P| \geq k$ ), we define the discrete  $k$ -median problem as follows. Find a subset  $C \subseteq P$ ,  $|C| = k$ , such that  $\text{cost}(P, C) = \sum_{p \in P} \min_{c \in C} D_{l_2^2}(c, p)$  is minimized. Denote the optimal discrete  $k$ -means cost by  $\text{opt}_k^{\text{discr}}(P)$ .

Let  $\text{opt}_k(P)$  be the optimal  $k$ -means cost of  $P$ . Prove that

$$\text{opt}_k^{\text{discr}}(P) \leq 2 \cdot \text{opt}_k(P).$$

**Exercise 2:**

Let  $S \subset P$  be an  $\epsilon$ -stable set of  $k$  centers, and let  $O \subset P$  be an optimal set of  $k$  centers. Prove that

$$D(P, S) \leq \left( \frac{9}{1 - \epsilon} \right)^2 D(P, O).$$