

## Clustering Algorithms

WS 2015/2016

Handout 8

### Exercise 1:

Given  $D = D_{l_2}$ , describe an instance  $P$  for which the GONZALESALGORITHM computes a solution  $C$  such that

$$\text{cost}_{\text{diam}}(C) = (2 - \epsilon) \cdot \text{opt}_{\text{diam}}^k(P)$$

for any  $\epsilon > 0$ .

### Exercise 2:

Prove that the GONZALESALGORITHM is a 2-approximation algorithm for the radius  $k$ -clustering problem.

### Exercise 3:

Let  $C, C'$  be two distinct density-based clusters of point set  $P$  wrt. to  $\epsilon$  and  $MinPts$ . Prove that the intersection  $C \cap C'$  of  $C, C'$  contains only border points.

### Exercise 4:

Consider the following version of the DBSCAN algorithm.

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- 1:  $C := \{p \in P \mid |N_\epsilon(p)| \geq MinPts\}$
  - 2:  $N := \{p \in P \mid |N_\epsilon(p)| < MinPts \wedge \nexists c \in C : D(p, c) \leq \epsilon\}$
  - 3:  $B := P \setminus (C \cup N)$
  - 4: Construct a complete graph  $G$  with nodes corresponding to  $C$  and weight each edge  $(c_1, c_2) \in C \times C$  by  $D(c_1, c_2)$
  - 5: Remove all edges of  $G$  with weight  $> \epsilon$
  - 6: Compute the connected components of  $G$
  - 7: **for** each connected component (denote its set of nodes by  $C_i$ ) **do**
  - 8:     Compute all distances between nodes in  $C_i$  and in  $B$
  - 9:      $C_i = C_i \cup \{v \in B \mid \exists c \in C_i : D(v, c) \leq \epsilon\}$
- return** Clustering  $C_1, \dots, C_k$  and  $N$  as set of noise points
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Show that this algorithm computes a valid density-based clustering.