## Fundamental Algorithms

WS 2017

## Exercise Sheet 7

## Exercise 1:

Show that there cannot be a graph $G$ of size $n$ with girth $>2 k$ and minimum degree $>\left\lceil n^{1 / k}\right\rceil$.

## Exercise 2:

Provide an efficient algorithm for the maximal matching problem and show its runtime.

## Exercise 3:

Show that every tree has at most one perfect matching.

## Exercise 4:

Compute of maximal matching of the following graph by repeatedly choosing any augmenting path $P$ and updating your current matching $M$ to $M \ominus P$.


