# Fundamental Algorithms WS 2017

# Exercise Sheet 7

# Exercise 1:

Show that there cannot be a graph G of size n with girth > 2k and minimum degree >  $\lceil n^{1/k} \rceil$ .

#### Exercise 2:

Provide an efficient algorithm for the *maximal* matching problem and show its runtime.

## Exercise 3:

Show that every tree has at most one perfect matching.

## Exercise 4:

Compute of maximal matching of the following graph by repeatedly choosing any augmenting path P and updating your current matching M to  $M \ominus P$ .

