

**Advanced Algorithms**  
WS 2019  
**Homework Assignment 9**

**Problem 22:**

Use randomized metric reduction in order to show that the TSP problem on  $n$  nodes whose pair-wise distances are given by any metric  $d$  has an approximation algorithm with an expected approximation ratio of  $O(\log n)$ .

**Problem 23:**

In the *communication spanning tree problem* we are given an undirected graph  $G = (V, E)$  with edge costs  $c : E \rightarrow \mathbb{N}$  and the goal is to find a spanning tree  $T = (V, E')$  of  $G$  that minimizes the sum of the pairwise distances with respect to  $T$  over all pairs of nodes. Show that there is an  $O(\log n)$ -approximation algorithm for this problem using the metric reduction approach.

**Problem 24:**

Prove Theorem 6.5 in Chapter 6 of the lecture notes.